Galaxy Clusters and Self Similarity I



About Me

- Dr Ben Maughan
 - Degree: Cardiff
 - Ph.D: Birmingham
 - Chandra Fellow: Harvard-Smithsonian Centre for Astrophysics
- Research:
 - X-ray properties of galaxy clusters
 - Cosmology
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Lectures

Tuesday 9.00	Wednesday 11.10	Thursday 12.10am
BJM	BJM	BJM

 Lecture material online: http://www.star.bris.ac.uk/bjm/lectures/topics

Course Outline

- Introduction to galaxy clusters and properties at different wavelengths
- Self similarity in galaxy clusters theoretical background and comparison with observations
- Observational results on similarity breaking and causes

Reading List & Exam

Read at least one of the following papers:

- Branchesi et al. (2007), A&A, 472, 739-748
- Kotov & Vikhlinin (2005), ApJ, 633, 781-790
- Lumb et al. (2004), A&A, 420, 853-872
- Magliocchetti & Bruggen (2007), MNRAS, 379, 260-274
- Exam consists of short and long answer question on each topic
 - answer all short and 2 long questions
 - full marks on my long question requires correctly referencing one paper above e.g.

"Maughan et al. (2007) showed that the scatter in the X-ray luminosity – mass relation is significantly lower than previously thought."

Today

Introduction to galaxy clusters

- Why so interesting?
- Properties at different wavelengths
 - Optical
 - Gravitational Lensing
 - Sunyaev Zel'dovich effect
 - Numerical simulations
 - X-ray

Galaxy Cluster Recipe



- Take approx $10^{15}M_{\odot}$ dark matter
- Marinade in approx $10^{14}M_{\odot}$ hot (10⁷K) ionised gas
- Sprinkle with 100's of galaxies of various shapes and sizes $(\sim 10^{13} M_{\odot})$
- Finished product approx 2Mpc in radius



Clusters & Cosmology

Early Universe was smooth with tiny density perturbations after Big Bang

- Density peaks amplified by gravity
- Galaxy clusters form via series of mergers of smaller systems – hierarchical formation
- Largest gravitationally bound objects in Universe



Simulation of development of structure in Universe. Circles show locations of galaxy clusters

Clusters & Cosmology

Growth of large scale structure traced by clusters

- Sensitive to cosmological parameters
- Clusters provide powerful tests of cosmological models

Flat Universe $\Lambda=0.7$

Flat Universe $\Lambda=0$



Clusters & Cosmology

Constraints competitive, independent and different degeneracies to other methods

Cosmological tests require cluster masses



Two principal reasons to study galaxy clusters:

- Measuring masses for cosmology
- Unique laboratories for interesting physical processes

Best cosmological constraints need **large samples** out to **high redshift**

Optical Properties

First studied in optical

- **100s or 1000s of member galaxies** Abell (1958) catalogue
- Detect clusters based on overdensities of galaxies
- Suffers projection effects
- Study richness and morphology of clusters



Optical Properties

Zwicky (1933) measured redshifts of galaxies in coma

- What is z of Coma? Why don't galaxies have same z?
- Velocity dispersion
- Velocity dispersion gives kinetic energy of galaxies
- Virial theorem gives ^z ³ total cluster mass
- Zwicky found <1% mass in galaxies
- First evidence for dark matter



- Deep gravitational potential in clusters acts as gravitational lens
- Distorts shapes of background galaxies
- Effect strongest in cores
- Arc like distortions & multiple images
 - "Strong lensing"



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Outside cluster cores, effect is weaker

 Subtle elliptical distortions to background galaxy shapes - "weak lensing"



and white sticks show mean

orientation of background galaxies

Can't measure distortion for a particular galaxy

Don't know what shape it was originally

Measure statistical distortions of many galaxies

 Will be random if no lensing signal

Both strong and weak lensing can be used to determine cluster masses

Sensitive to all mass along line of sight



Affected by mass in large scale structure around clusters

Introduces uncertainties

and white sticks show mean orientation of background galaxies

Sunyaev-Zel'dovich effect

Microwave background photons are inverse Compton scattered to higher energies by electrons in ICM

HOT

 $(1 - 1)^{500}$ $(1 - 1)^{20}$ $(1 - 1)^{200}$

Strength of effect depends on T and ρ of ICM, but is independent of redshift!









MICROWAVE BACKGROUND

PHOTON

Distorts shape of CMB spectrum – intensity drops at lower frequencies

Numerical Simulations of Clusters

Computer simulations allow testing of cluster models, include dark matter

- What physical processes must be included in simulations to match observations of real clusters?
- Simulations also allow study of dynamics of clusters on timescales too long for direct observation



Summary

- Galaxy clusters studied at different wavelengths:
- Optical
 - Galaxy velocity dispersions, richness, morphology
- Gravitational lensing
 - Strong and weak lensing can give cluster masses
- SZ effect
 - Sensitive to ICM properties, independent of z
- Simulations
 - Formation & which physical processes important
- X-ray...

XMM-Newton 1999-

- 3 X-ray telescopes each with 58 nested Wolter mirrors
- Effective area approx 0.4 m²



XMM-Newton 1999-

- 3 X-ray telescopes each with 58 nested Wolter mirrors
- Effective area approx 0.4 m²
- 3 CCD cameras
- 2 diffraction gratings for improved spectroscopy
- ESA mission



Chandra X-ray Observatory 1999-

Single X-ray telescope with 4 nested Wolter mirrors

- Effective area approx 0.1 m²
- Lower sensitivity than XMM-Newton
- PSF of 0.5 arcsec compared to 15 arcsec for XMM
- CCD camera and diffraction grating



X-ray Properties

Galaxy clusters first detected as X-ray sources in 1966 using rocket-based detectors

- Source of emission initially debated
- Better data showed bremsstrahlung emission from hot, ionized gas
- Free-free emission from electrons accelerating around ions
- Highly luminous X-ray sources



X-ray Properties

Emissivity of a bremsstrahlung-emitting plasma is:

$$\varepsilon_{v} \propto \frac{Z^{2} n_{e} n_{i}}{T^{1/2}} e^{-\left(\frac{hv}{kT}\right)}$$

 ϵ = energy emitted per unit frequency, time and volume n_e , n_i = number densities of electrons and ions

Z = charge on ion, T = temperature, v = frequency

The luminosity of the intra-cluster medium (ICM) is given by integral of ϵ over all frequencies and then over volume of cluster

$$L_X \propto \int n_e n_i T^{1/2} dV \qquad (1.1)$$

- Depends strongly on $\rho,$ more weakly on T

X-ray Properties

- Intensity of X-ray emission $\propto \rho^2$
- High X-ray luminosity (Lx) means clusters detectable to high z
- Large samples of clusters detected in X-ray surveys



X-ray Spectra

- X-ray emitting gas (ICM) composed of H, He, and trace heavier elements
- X-ray spectra of ICM show continuum from bremsstrahlung and line emission from e.g. Fe, Si
- Metal abundances indicate ICM been processed through stars



X-ray Spectra

- Models fit to observed X-ray spectra give temperature (kT) of the ICM
- kT in range 1 to 15 keV



- Gas heated to these temperatures during cluster formation
- kT gives mean KE of gas particles
 - Apply virial theorem to give cluster mass
- Again, dark matter is required

X-ray kT Profiles

- Measure kT in several annular regions if data is good enough
 ^{r, arcmin}
- Gives kT and its gradient as a function of radius





X-ray Surface Brightness Profiles

- Surface brightness profiles show the distribution of the ICM density
- Fit model to observed SB profiles to recover ICM density and its gradient as function of radius





CAUTION! Projection Effects

- Observed surface brightness and kT profiles are a projection along line of sight of the true 3D emission
- When we look at centre of cluster we are looking through outer parts of cluster too $$\wedge$$
 - contributes to measurements







Hydrostatic Equilibrium

 If the ICM is in hydrostatic equilibrium with total gravitational potential (pressure balances gravitation):

$$M(r) = \frac{-r^2}{G\rho(r)} \frac{dP}{dr}$$

• Which, for an ideal gas gives:

$$M(r) = \frac{-r^2 k}{G \mu m_p \rho(r)} \left[\rho(r) \frac{dT}{dr} + T(r) \frac{d \rho}{dr} \right]$$

 So measuring T(r) and ρ(r) of gas allows us to derive M(r) for total mass including dark matter

Example: Hydrostatic Equilibrium

Starting with eqn hydro eqm, and using ideal gas law (PV = nRT = NkT) show that

$$M(r) = \frac{-r^2 k}{G \mu m_p \rho(r)} \left[\rho \frac{dT}{dr} + T \frac{d \rho}{dr} \right]$$

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$$M(r) = \frac{-r^{2}}{G\rho(r)} \frac{dP}{dr} \quad \text{(a)} \qquad PV = NkT = \frac{M_{gas}}{\mu m_{p}} kT$$

Where μ is mean atomic mass per particle & m_p is proton mass

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$$P = \frac{\rho kT}{\mu m_p} \qquad \qquad \frac{dP}{dr} = \frac{k}{\mu m_p} \frac{d}{dr} (\rho T) = \frac{k}{\mu m_p} \left[\rho \frac{dT}{dr} + T \frac{d\rho}{dr} \right]$$

substitute into (a):

$$M(r) = \frac{-r^2 k}{G \mu m_p \rho(r)} \left[\rho \frac{dT}{dr} + T \frac{d \rho}{dr} \right]$$

Summary of X-ray Properties

- X-ray observations of galaxy clusters allow us to measure these key properties:
 - X-ray luminosity (from images or spectra)
 - kT of the ICM (from spectra)
 - Metal abundances in ICM (from spectra)
 - Density of ICM (from surface brightness profile)
- Combining radial profiles of kT and p of ICM we can infer total mass assuming hydrostatic equilibrium

Galaxy clusters consists of

- Dark matter (~80%), hot gas (~15%), galaxies (~5%)
- Galaxy cluster studies important for
 - Measuring cluster masses for cosmology
 - Investigating physical processes in clusters
- Observations at different λ and simulations used
- X-ray observations particularly powerful
 - Detect clusters to high-z
 - Measure ICM properties
 - Infer total cluster mass